

AN IMAGE-BASED FOCUSING SYSTEM

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### Abstract

Hardware simulating a retina was developed to test whether lateral inhibition is an adequate processing basis for the determination of best focus in a dense sensor imaging system on flat fields. The system developed shows that maximizing the sum of adjacent sensor light level differences is an adequate algorithm for focusing on a wide range of visual stimuli.

The hardware was developed as a prototype image focusing and retrieval system. A Reticon light sensitive array (Reticon RL256G) is used as the sensing element. An Intel 8085 based computer with limited memory (512 bytes ROM, 512 bytes RAM) is used to process the data. The system automatically focuses on stimuli in object planes. It can also manually focus, input images and take light level and spatial frequency measurements of scenes.

Besides being well suited for studying ocular contrast difference judgments and computational problems of image interpretation, this system is appropriate for video and film applications. On a movie or video camera, the system could meter light, focus and in many cases track specific moving objects. This would give the camera operator increased control of a scene.

INTRODUCTION

Ocular focus for humans and animals is in most cases an unconscious effort. Only in the case of organic disabilities do people have trouble focusing on stimuli in normal visual experiences. With effort, people can defocus the image falling on their retina. This paper describes a project which explored:

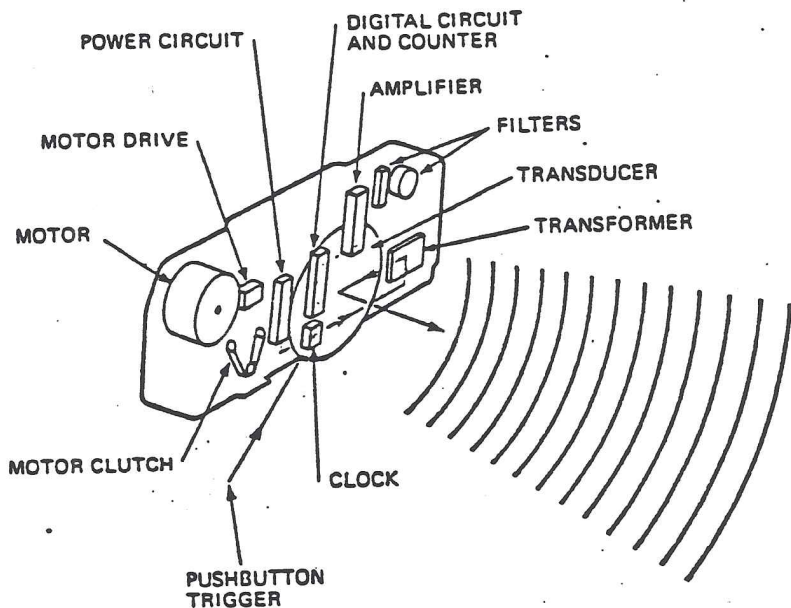
- 1) What does "best focus" mean?
- 2) What is the simplest processing required to use information from an image in order to optimize an object's focus through a lens?
- 3) What is the difficulty of constructing a focusing aid designed to save video camera operators effort?

Two automatic focusing systems are now commercially available (Figure 2). Honeywell announced their "Visi-tronic" automatic rangefinder style focuser in 1978. This system uses 4 matched pairs of light sensors located behind a special rangefinder-style mechanical and optical setup. Comparators signal a solenoid to move a rangefinder mirror and lens to correlate light levels on matched sensors. Polaroid introduced a sonar-focusing measurement system on a new line of cameras in the same year. Their system reflects a focused beam of ultrasonics off of an object and measures its travel time to determine object distance. Neither of these focusers is self-calibrating; neither relies on the

# Two Commercially Available Non Image Based

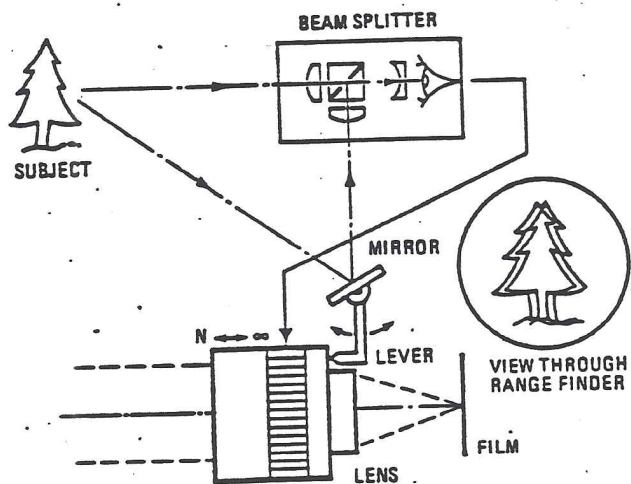
Figure 2

## Focusing Systems



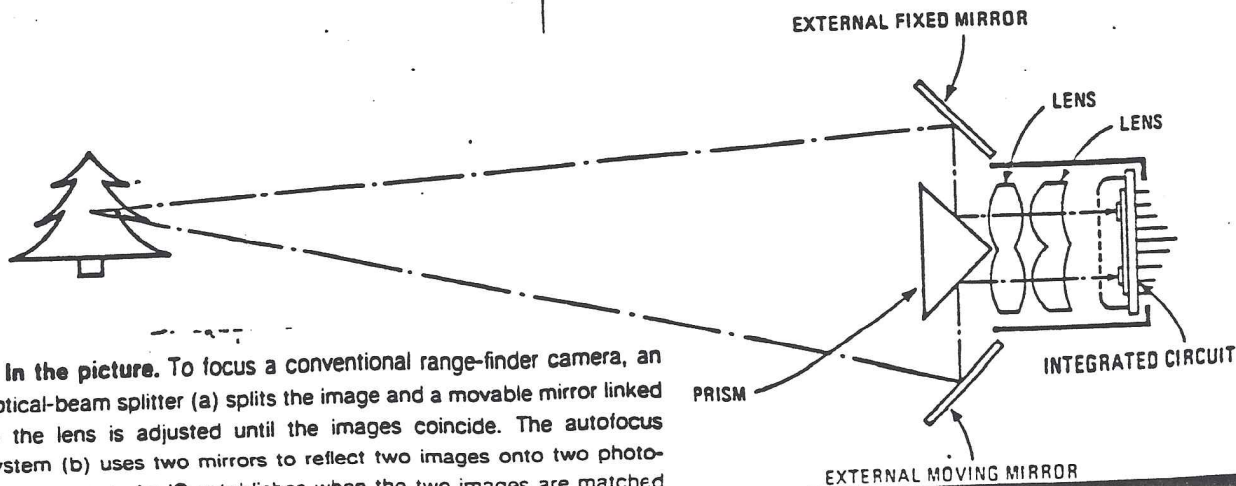
POLAROID

Ranger. Sound waves created by electrostatic transducer helps new camera find range. Motor focuses lens according to time for sound to hit target and return.



HONEYWELL

(a)



1. In the picture. To focus a conventional range-finder camera, an optical-beam splitter (a) splits the image and a movable mirror linked to the lens is adjusted until the images coincide. The autofocus system (b) uses two mirrors to reflect two images onto two photo-sensor arrays. An IC establishes when the two images are matched

actual image projected.

An image-based focusing system uses the image projected through a lens as its database. To focus using this information one needs to understand focus. Ideal focus exists when the light level (which we will call luminescence) distribution function on the image plane varies from the stimulus (object) plane's luminescence distribution only by coefficients of enlargement and brightness. In this condition with a magnification of 1, object plane points would map directly onto image plane points. Defocus is characterized by points in the object plane mapping onto a distribution area about the place where the focused point would map in the image plane. This area is what we call the blur-circle on the defocused image. The luminescence (L) on the image plane corresponding to a light point of light level (E) on the object plane can be described as

$$L = E \frac{1}{(2 \pi (3\theta))} e^{**\langle -1/2(r**2) / (3\theta)**2 \rangle} .$$

R is the distance away from the center of the area to which an object point is mapped and  $\theta$  is the distance (r) at which 67% of the light is within r. (Blur Of The Retinal Image, page 14). The larger the blur-circle is, the worse the focus. This blur affects different scenes in different ways.

If an object plane is all one luminescence, it is not possible to determine ideal focus. The redistribution of object plane light points onto image plane blur-circles will only change the source of image light, not the actual image light level. Light from adjacent object plane points will overlap in the image plane. Since these all have the same intensity, no fluctuations in light level will be introduced.

The next simplest focus problem, that of 1 light level change, can be most easily considered in the one-dimensional image plane. Consider an image plane which is a line. If part of it is light and part of it is dark, there will be only 1 light level change in ideal focus; that of the interface (Figure 3A). This change is equal to the difference in brightness of the two parts of the stimulus. If the system is defocused, blur-circles of all points from light side within blur-circle radius of the interface will map their light to the dark side of the interface. There will a gradient of light level change about the interface. Within this radius on either side of the interface, the light level will be changed; the light side darkened as well as the dark side lightened. Contrast (change in luminescence with respect to distance divided by luminescence) is decreased. For points along the line far enough away from the step light level change, light level is unaffected. If the blur-circles from the step light change map off the image

plane, the total light level change along the line will be decreased.

A more complicated situation consists of two opposing light level changes along the one-dimensional image plane. A good example of this is a bar of light (Figure 3B). In this case, if the blur-circle caused by defocus is larger than  $1/2$  the width of the light bar, the maximum light level of the bar in the focus condition will not be attained. In this case all points on the light section spill light onto the dark sections. If the image projection of the bar is within blur-circle radius of either edge of the image field, the maximum darkness of the focused condition will not be attained either. In all of these defocus cases, the sum of the absolute values of light level changes along the image plane is decreased. Even in the cases where defocus does not cause a decrease in absolute light level changes, it does decrease contrast.

We call the sum of the absolute value of light level changes along the image line the Luminescence Difference Sum (LDS). The sum of squares of the differences of light level change across a scene will be decreased with defocus even for simple decrease in contrast. We call this the Luminescence Difference Square Sum (LDSS). The more complicated an object stimulus is, the higher its spatial frequency and the easier it is to see change in the LDS with

# SIMPLE EXAMPLES: FOCUS Figure 3

SIMPLEST CASE ONE DARK TO LIGHT EDGE

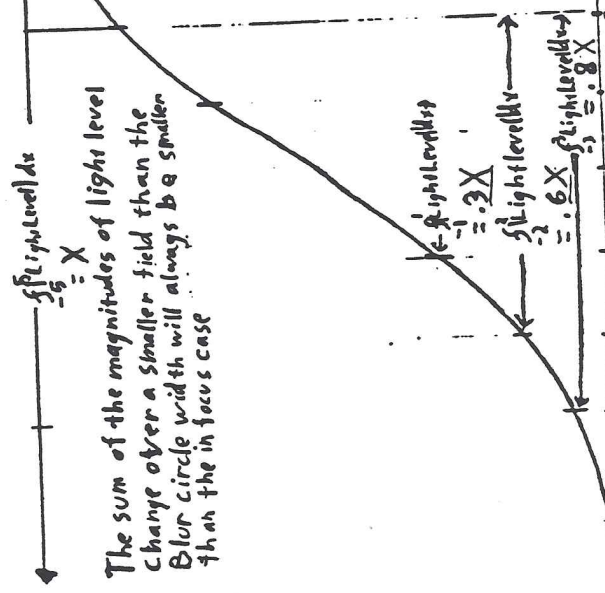
INFOCUS

$LDQ \approx \sum |\Delta \text{Light level}| dx$   
 = Sum of the magnitude of  
 Light Level differences  
 = X

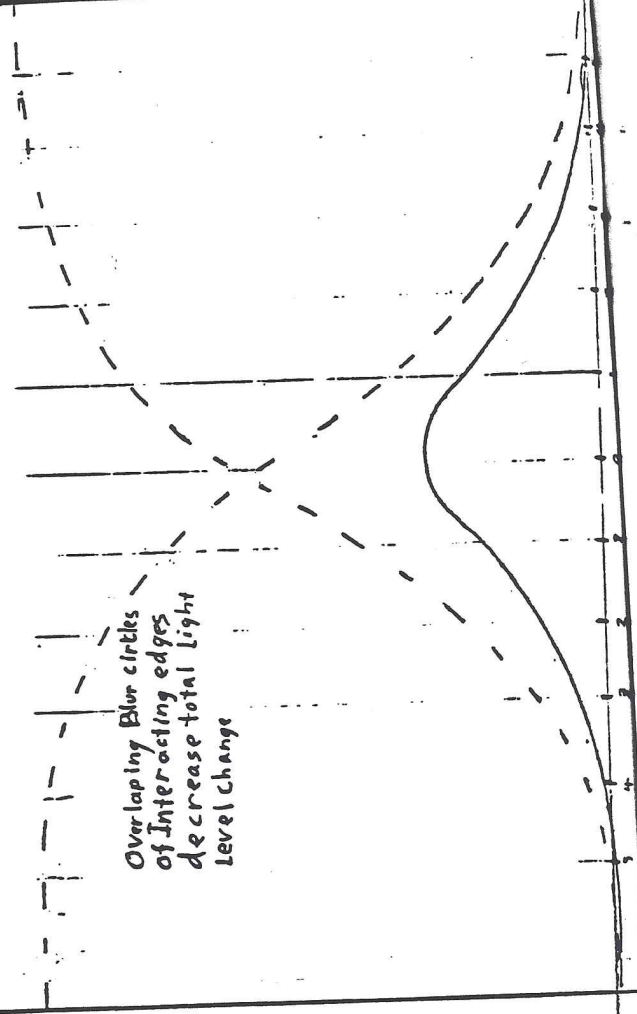
TWO EDGES INTERACT: DARK TO LIGHT TO DARK

$LDQ = \text{magnitude of Dark to Light Ed} + \text{magnitude of Light to Dark}$   
 $= 2X$

OUT OF FOCUS



Overlapping Blur circles of Interacting edges decrease total Light Level change





defocus. For most real life focus problems it appears that that maximizing this LDS gives best focus.

For an array of discrete detectors such as a retina, an adequate algorithm for focus simply takes the LDS over the array and maximize it by changing focus. A system was built to test this hypothesis and to explore uses of it.

METHOD

A focusing system was conceived to simulate human methods of focusing in an artificial retina. Investigative purposes included: testing a model we had proposed concerning a possible way in which animal ocular systems focus themselves, creating a general-purpose versatile focusing and imaging system capable of tracking focusing, and analyzing scenes. Several configurations for the "retina" were proposed:

- 1) A tightly packed arrangement of light sensing diodes would allow parallel outputs which could be processed like that of a retina. In this system the outputs of adjacent light sensors would be physically connected to layers of parallel circuitry. This circuitry would first introduce lateral inhibition (the tendency for stimuli presented next to a sense field to decrease its sensitivity) between sensors. This sensing circuit would then have a contrast sensitive output.
- 2) Improved sensor density could be realized by feeding the sensors with a fiber-optics bundle. with a fiber-optics bundle to increase the resolution of the image. Closely packed fiber ends would map to widely spaced light sensitive diodes.
- 3) Another sensor was also considered which utilized a serially addressable diode array as a high density central vision area and discrete devices for peripheral area These

areas correspond to areas in the human eye.

4) A simpler system with one densely packed horizontal line of 256 sensors using a Reticon RI256G was a compromise.

While more physiological, parallel-processing models can only be tested with discrete elements, they can be simulated with a serial device. The computational problems for a two-dimensional input would be impossible to handle with the computers readily available; hardware realizations would be equally impractical. The Reticon serially addressable array was chosen. It has light-sensitive diodes mounted every 15 microns for 0.25 inches. Other horizontal hardware configurations could be simulated using it.

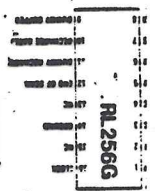
HARDWARE

To become familiar with the Reticon array, more than one method of data acquisition was tested. Measuring the voltage level on the sensors is the most stable, versatile output (but the hardest to arrange). Measuring the current discharge of each sensor is easier but less useful. First a circuit to display current discharge of each element on an oscilloscope was set up.

The Reticon chip consists of a shift register whose 256 outputs are connected to Metal Oxide Semiconductor (MOS) switch transistors. Light sensitive diodes deposit charge on capacitors. When the MOS transistors are off, the sensors are isolated from the rest of the circuit. When an MOS switch transistor is turned on, charge deposited on the associated junction capacitor is connected to the outputs of the chip. At the same time, these are connected to identical outputs for reference purposes. The chip addresses one of these sensors at a time. This allows them to charge for 255 cycles before being read. Another identical set of sensors not exposed to light is selected in parallel with the light sensitive array. The outputs from this array are subtracted from the signal to eliminate timing noise. The output data line of the chip goes through 2 MOS transistors. The data line is connected to the gate of a buffer transistor for high impedance voltage measurements. The data line

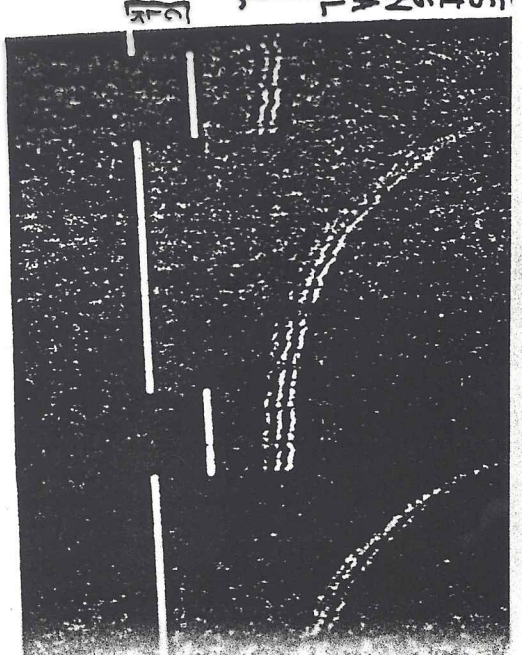
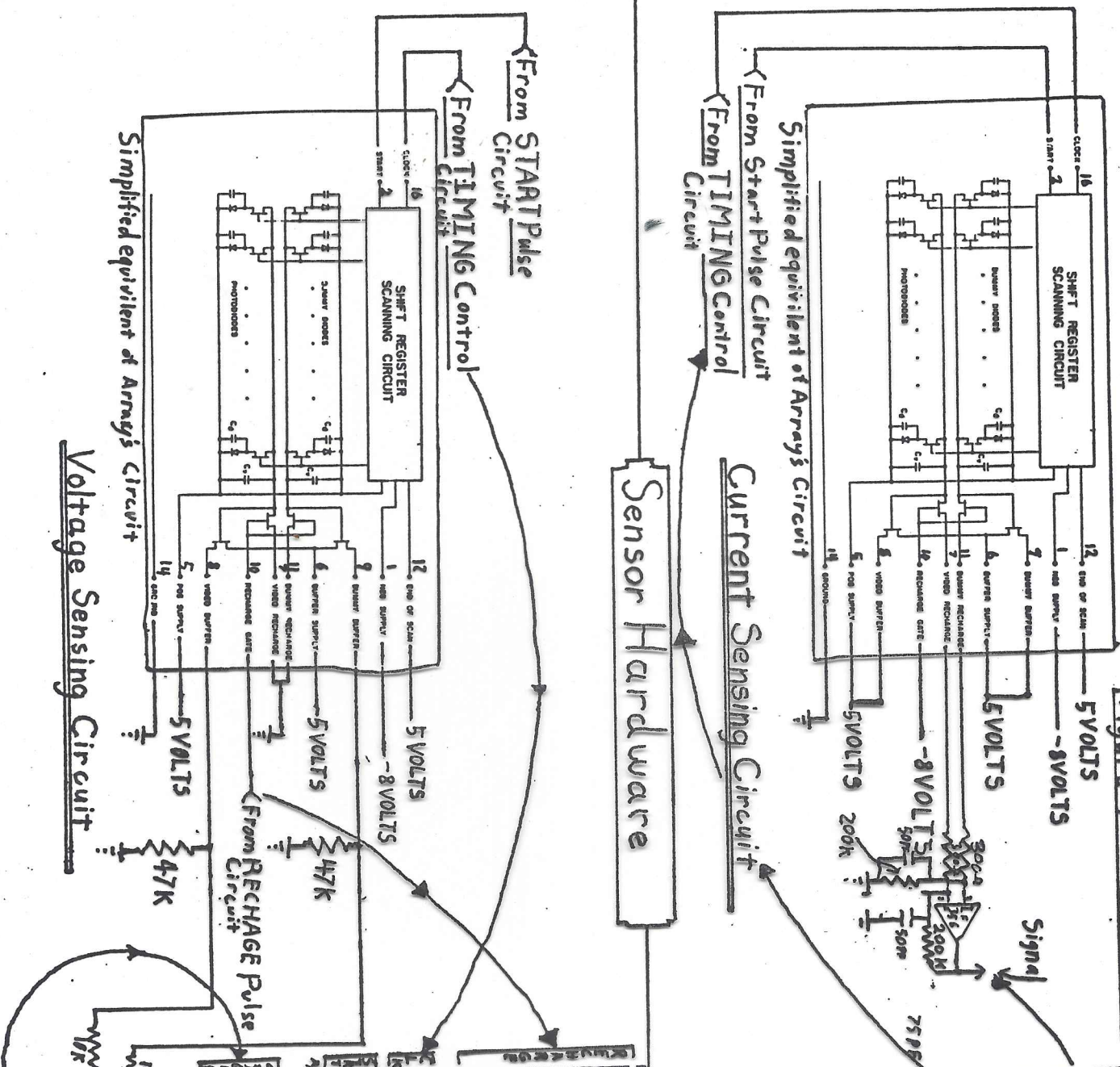
is also connected to the source of a recharge gate to remove the light-deposited charge from the sensor junction capacitors each time they are read. Since the array only addresses a specific sensor once every 256 cycles, the sensitivity is inversely proportional to the speed of the clock and directly proportional to the time the sensors have to charge between readings. If this array scan time is over 1/30th of a second, however, noise rises above 1/10 of signal level and the light level data will have significant offset error. Each of the 2 methods of extracting data from the array uses its circuitry differently.

For the current sensing method of data acquisition, chip drive requirements include: a start scan pulse, a clock pulse, and a difference amplifier for output (Figure 4A). A Tektronix signal generator was used for the clock pulse generator. Two 4 bit up-down counters (74192's) were used to divide the generator's output by 256 to serve as a start pulse. An LF256 instrumentation amplifier was used as a buffer and difference amplifier between the dummy diode and the data diode output current. These currents were sensed across load resistors. The buffer transistor supplies were wired off and the recharge gates were biased on. The load resistor was connected directly to the drains of the recharge buffers. Using this system the sensitivity of the array was shown to be within acceptable tolerance of the manufacturer's specifications. It is difficult to obtain

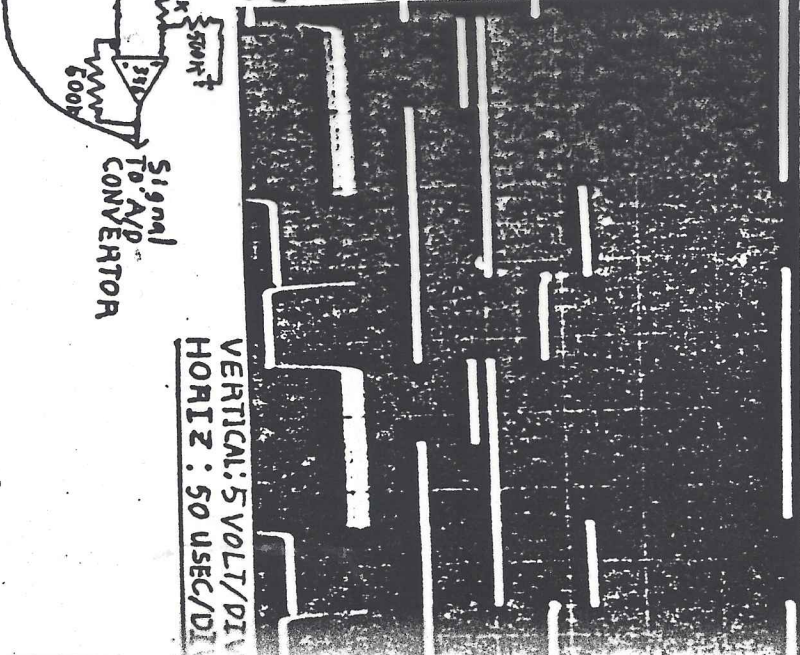


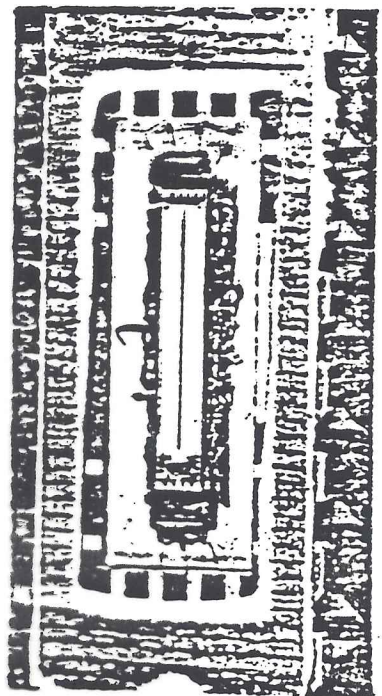
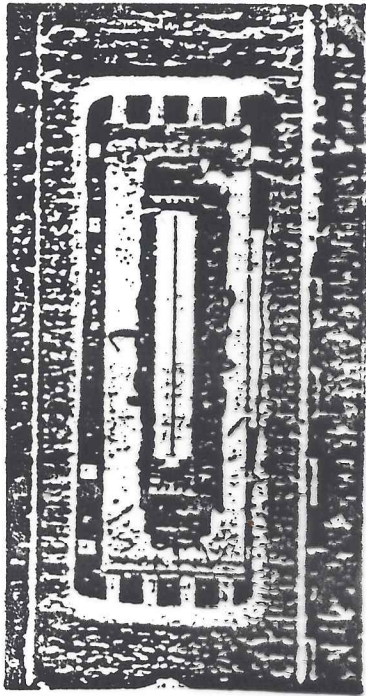
RL256G

Figure 4



VERTICAL: 5 VOLT/DIV  
 HORIZ: 50 USEC/DIV





stable samples using the current sensing technique of reading the array, it was hoped that using the voltage sensitive system would improve performance.

A circuit was designed to put a voltage level on a data line to correspond to illumination of sensing elements of the RL256G (Figure 4B and Figure 5). The charge potential across sensing diodes can be measured without discharging them. The high input impedance dataline buffers onboard the LF256 are ideal for this. For this purpose, these MOS buffers are simply biased to quiescence and read across a load resistor. The recharge transistors are pulsed negative at the end of the read cycle for each of the 256 sensing diodes. This pulse makes the data-line negative and recharges the 2 picofarads capacitor on the sensor diode being addressed. The array is read serially. When an element is addressed, it is first read through the buffers. By pulsing the 2 recharge gates with -8 volts, the junctions can be reinitialized before going on to the next element. The clock pulse in this system was one output of a 4 bit shift register (7495) circulating a bit. The bits purposes (in order) are:

- 1) to clock Reticon array,
- 2) to start Analog to Digital Converter,
- 3) to indicate that data is ready to be read,
- 4) to recharge the Reticon elements.

An NPN transistor inverts the 5 volt recharge pulse from the



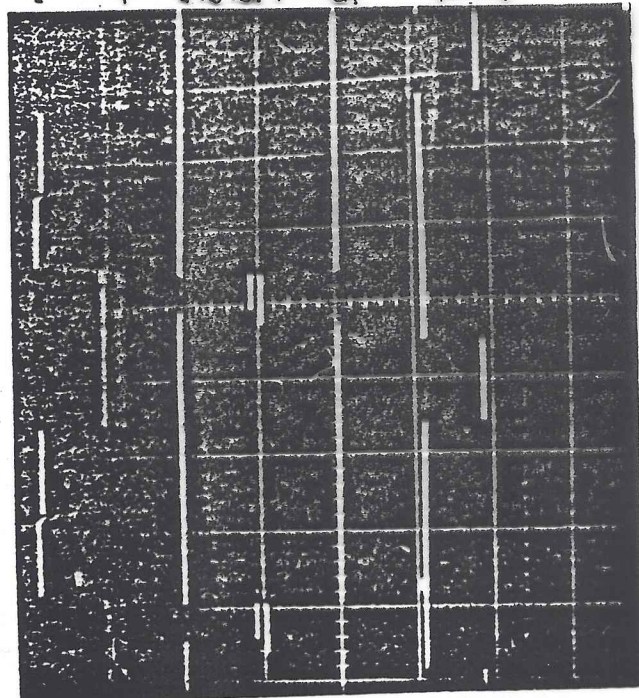
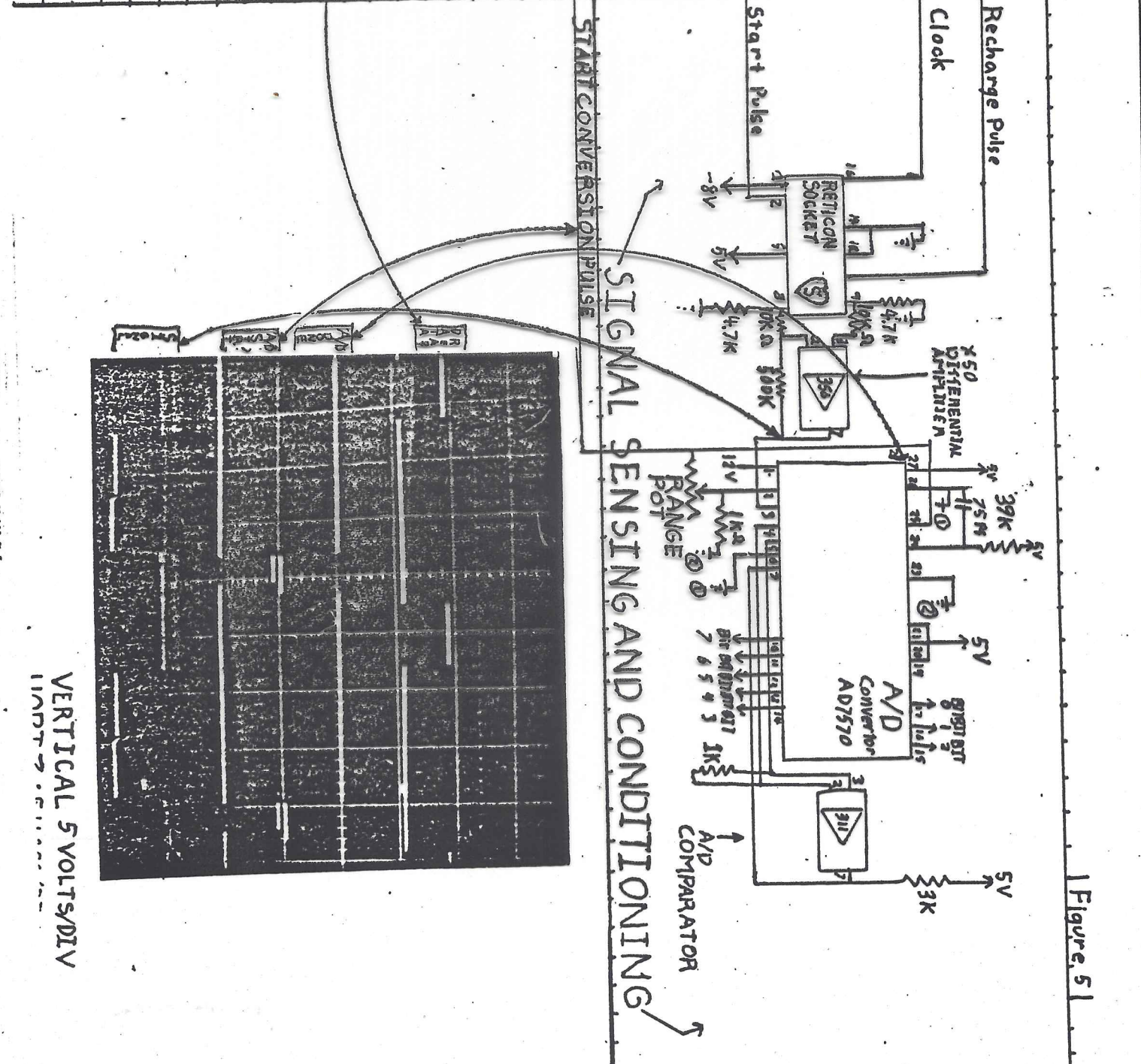
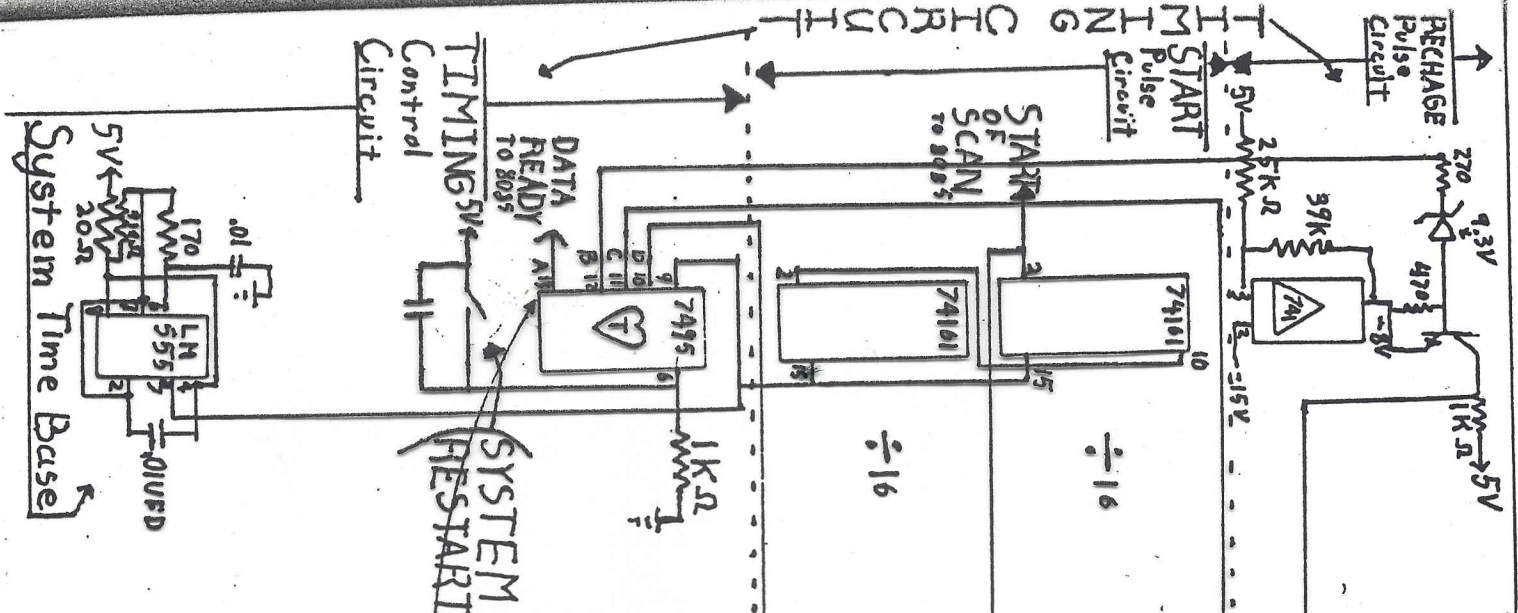
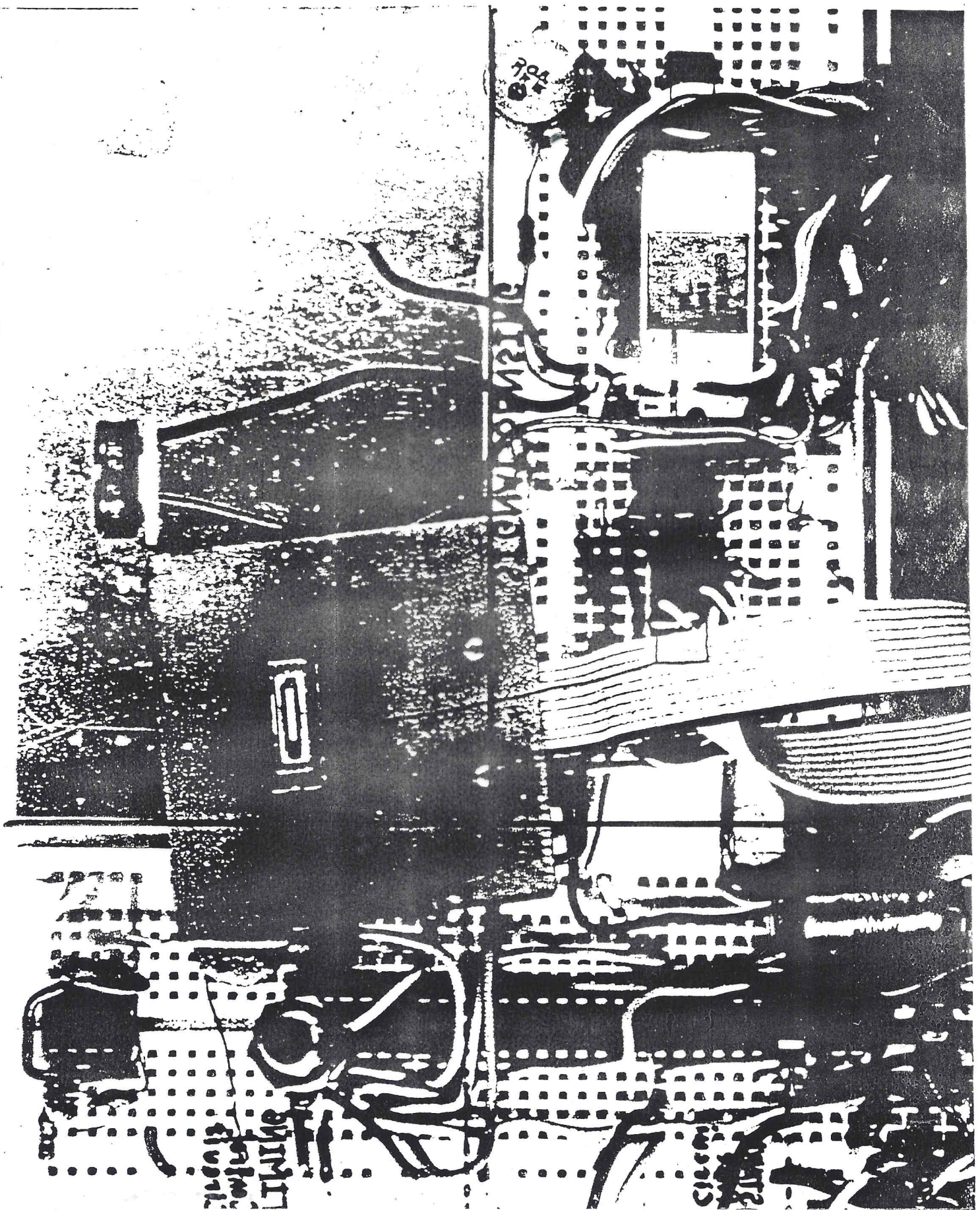


Figure 5

VERTICAL 5 VOLTS/DIV  
HORIZONTAL 100 NS



shift register to make a

-8 volt pulse to activate the recharge transistor.

The signal is sensed through the buffer transistor by applying 5 volts to the buffer's source and sensing across a grounded resistor. Optimal signal was obtained when this resistor was 4700 ohms. Even when maximum swing was assured by correctly biasing the Field Effect Transistors, the maximum voltage signal output was only .15 volts. The literature had claimed that one could expect up to 3 volts to accumulate on the diodes. The current sensing setup had indicated that the sensor followed the literature specifications. The possibilities of a damaged array, damaged buffers or damaged array elements were all tested.

The array elements' sensitivity was determined empirically, using a laser source and then more completely using a tungsten light (2870 degree Kelvin) (Figure 6). Sensitivity and linearity were both confirmed to be well within acceptable tolerance of the manufacturers specifications. A movable slit was arranged to demonstrate that the shift register was working. The buffer transistors were characterized by connecting a variable voltage to the activated recharge transistors and sensing the output voltage. In this way it was determined that these transistors both worked; they had acceptable leakage and gain characteristics. The recharge transistors were determined to work by measuring current

# RETICON ARRAY DIODE LINEARITY TEST

Figure 6

Since light intensity is inversely proportional to the square of distance from the light source, current charge on a light sensitive diode should be proportional to light intensity.

$$X = \text{Log } r$$

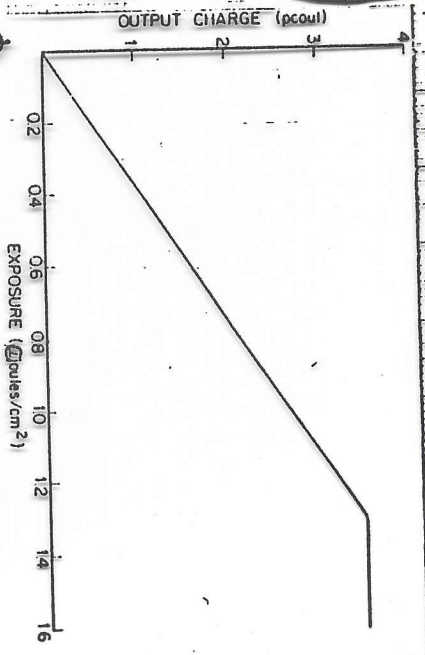
$$Y = \text{Log } I$$

Distance from light source (cm)

Light intensity (microamps)

RAW DATA

Distance from light source (cm)	Light intensity (microamps)	Video Charge Current (uamps)
10	1.75	2.42
20	.45	1.22
30	.183	.45
40	10.9	.225
50	7	.141
60	4.8	.094
70	3.5	.066
80	2.7	.051
90		.040
100	1.76	.03
110		.024
120	1.2	.018
130		.015
140	.97	.012
150		.009
160		.008
170	.665	.007
180		.006
190		
200	.44	
210		



This should give a linear plot with a slope of -2 on a graph where

$$L \cdot \frac{1}{r^2} = K \cdot I$$

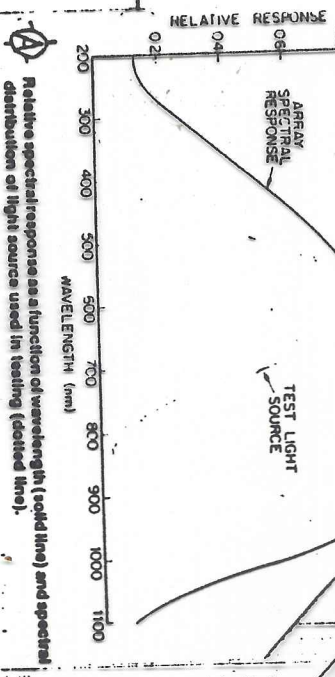
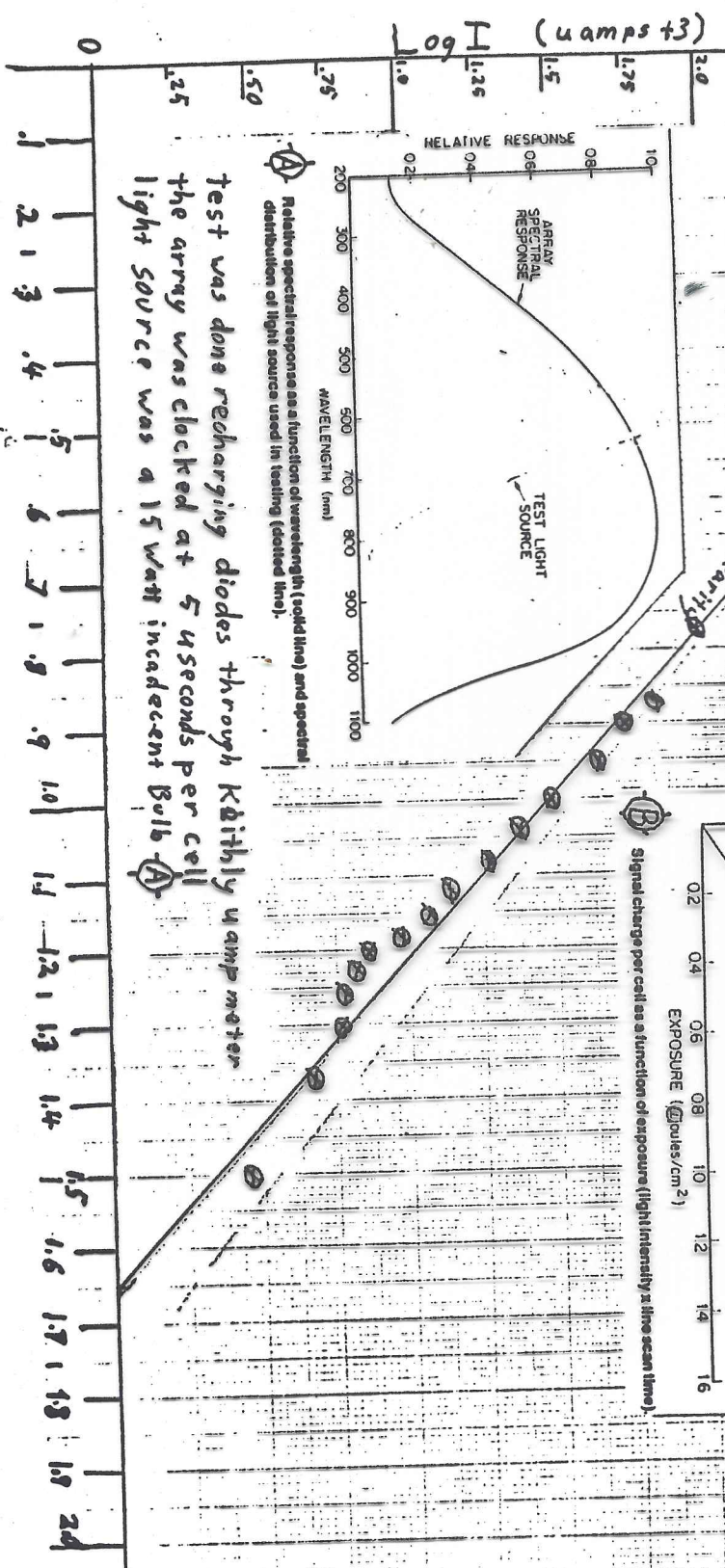
$$\frac{1}{r^2} = L \cdot K \cdot I$$

$$\frac{1}{r^2} = C \cdot I$$

$$\text{Log } \frac{1}{r^2} = \text{Log } (C \cdot I)$$

$$-2 \text{ Log } r = \text{Log } C + I$$

Signal charge per cell as a function of exposure (light intensity x time scan time).



Relative spectral response as a function of wavelength (solid line) and spectral distribution of light source used in testing (dotted line).

Test was done recharging diodes through Keithly wamp meter the array was clocked at 5 useconds per cell light source was a 15 watt incandescent bulb.

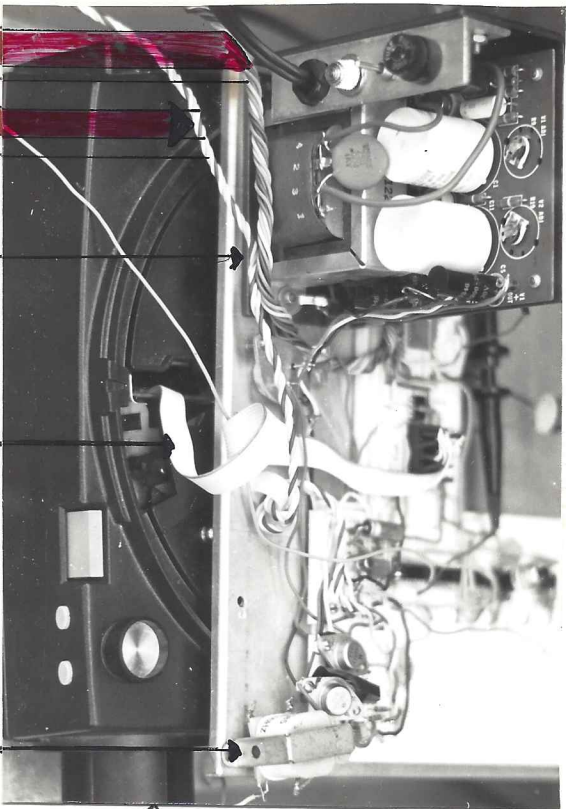
Log r (cm<sup>-1</sup>)

versus reset voltage during a completely saturated light level situation. Eventually it was realized that the junction capacitance of the diode capacitor was about 1/20 the capacitance value of the circuit reading its charge. The redistributed charge's potential decreased the signal by a factor of 20. The 0.15 volt Reticon signal needs conditioning to be used. It is necessary to subtract the dummy signal in order to cancel characteristic timing noise. The signal also has to be amplified to match the 0-10 volt input range of the Analog to Digital Converter. This converter produces a digital signal suitable for input to a computer.

The video and dummy signals of the Reticon array are combined in a high slew rate differential amplifier (LF356), which amplifies the combined signal to match the range of the next stage, the Analog to Digital Converter.

An Analog Devices AD7570J Analog to Digital Converter is used to convert the elements' relative output level to an 8 bit number. The chip was chosen for its speed and was run off its own clock with a cycle time of twenty microseconds.

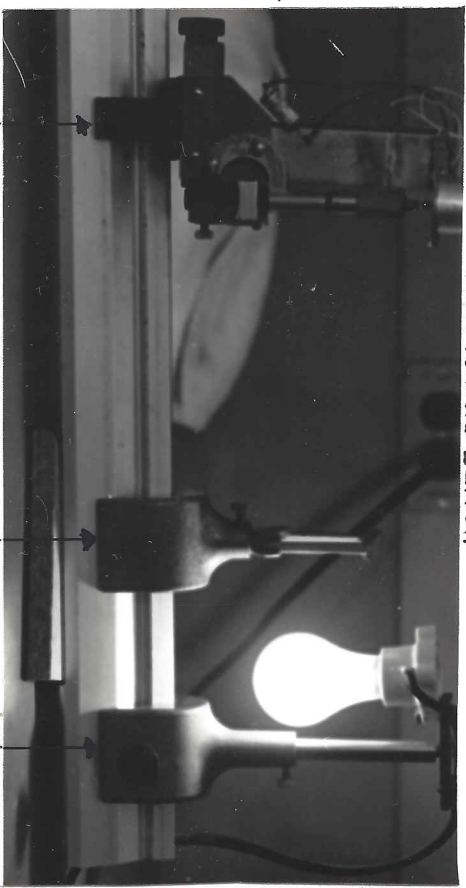
The optics and focusing motor from a 750H Kodak carousel projector was chosen to project an image onto the array (Figure 7 shows the system configuration). The array was mounted on a piece of fiberglass in the shape of a 35mm slide holder. In this way light projecting into the front



POWER SUPPLY  
CABLE TO ARRAY  
MOTOR NOISE CHOKE

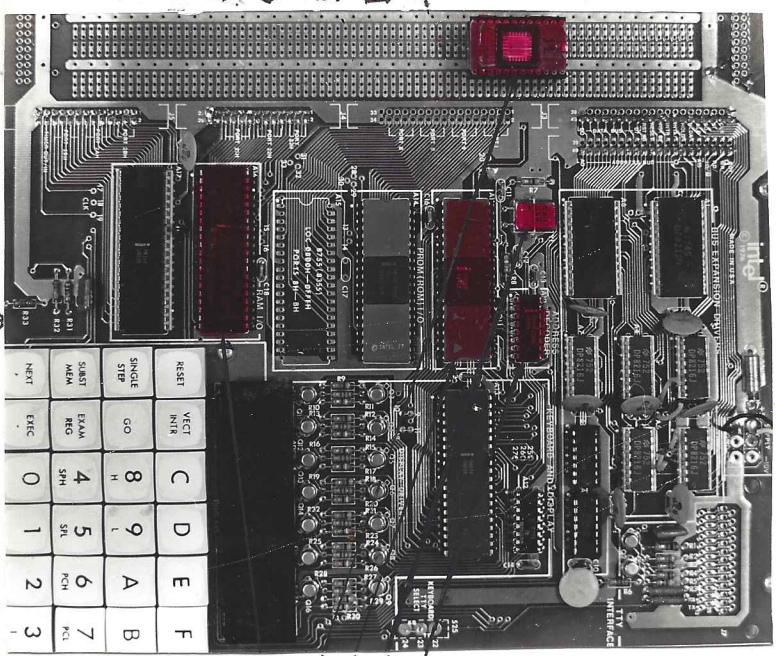
LENS

SYSTEM CONFIGURATION Figure 7



STIMULUS SLIDE HOLDER FITTED WITH STEPPING MOTOR FOR 2 D IMAGE COLLECTION  
DIFFUSOR TO ADJUST LIGHT LEVEL  
DC LIGHT SOURCE FOR EVEN LIGHT

ESSENTIAL FOCUS COMPUTER COMPONENTS  
ADDRESS DECODER  
TIME BASE  
8085 CPU  
5104 ROM FOR PROGRAM  
8155 I/O PORT, RAM



MCS 8085 DEVELOPMENT SYSTEM

DATA BUS Port 2A  
START OF SCAN PULSE Port 2B  
MOTOR DRIVE SIGNAL Port 29  
DATA READY PULSE Port 23

RESET	VECT INTR	C	D	E	F
SINGLE STP	GO	8	9	A	B
SRST MEM	EXAM REG	4	5	6	7
SRST	SR	0	1	2	3
EXIC					

of the projector could be accumulated from the position of a normal slide. The projector has a 102 mm lens on it. The 4.02 inch focal length determines the angle of visual field which will project onto the 0.25 inch photosensitive array when the lens is focused at infinity. This gives a field with an

$$\text{arc} = \arctangent \frac{0.25}{4.02} = 3.56 \text{ degrees.}$$

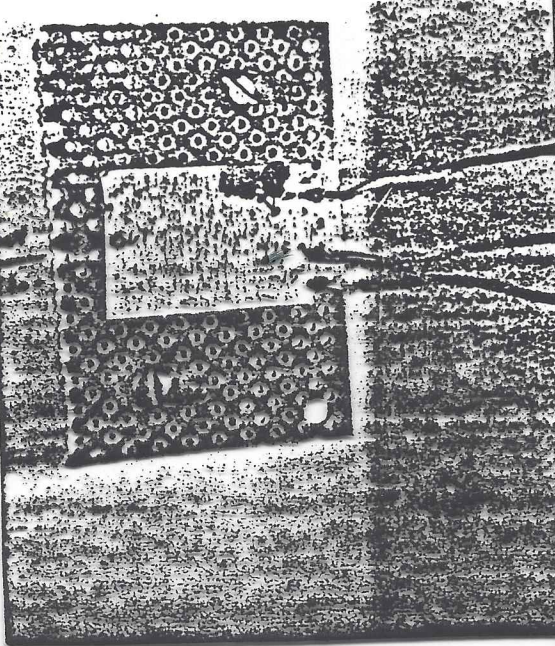
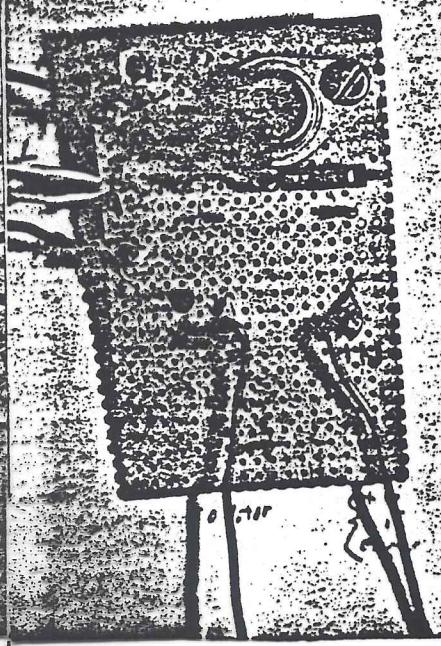
To use a 35 mm slide as the object plane it had to be positioned a distance

$$= \sin(3.56) 35\text{mm} = 1.5 \text{ feet away from lens.}$$

The focus motor requires +12 and -12 volts to move it forward and backward (see Figure 6). A 2 bit Transistor Transistor Logic (TTL) compatible driver was needed to use the 8085 TTL compatible output ports to drive the focus motor either direction or keep it still.

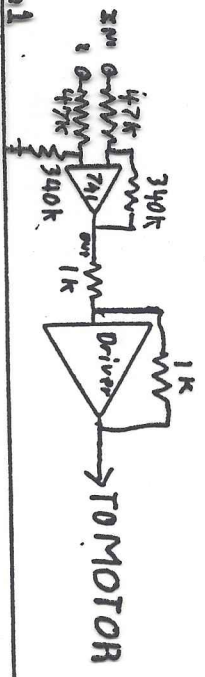
Using both inputs of a 741 in a difference amplifier configuration with an amplification of 3, both inputs low or both inputs high drove the motor with 0 volts. With the positive input of the amplifier high and the negative input low, the motor was driven with 12 volts. With the negative input of the amplifier high and the positive low, the motor was driven with -12 volts. Since the 741 cannot handle the full 120 milliamperes load of the motor, a monolithic driver amplifier was used to drive the motor (Figure 8A). This expensive device was replaced with VFET transistors (Figure 8B). These were found to be temperamental. The application

Figure 8

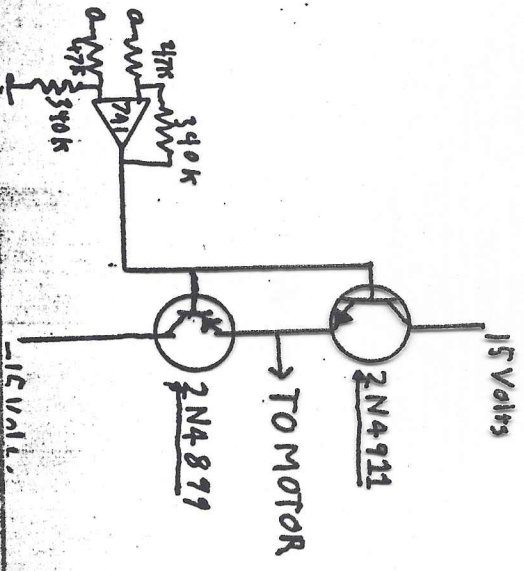
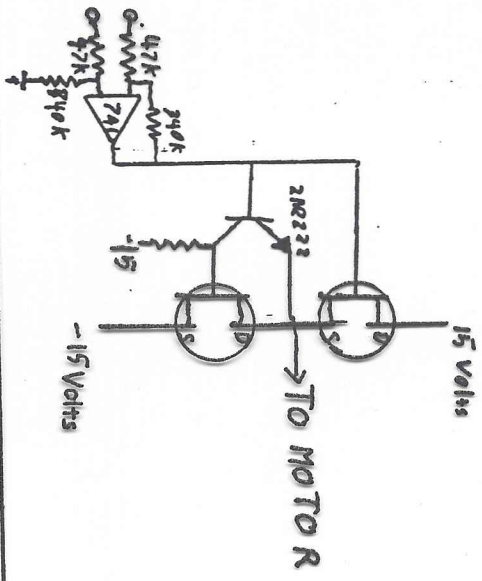


3 DIRRECTIONAL MOTOR DRIVER  
 INPUT: Zero -or- One TTL, 2 Bits  
 OUTPUT: 12 VOLTS, -12 VOLT S.a.O  
 120 Milliamps

Design 1



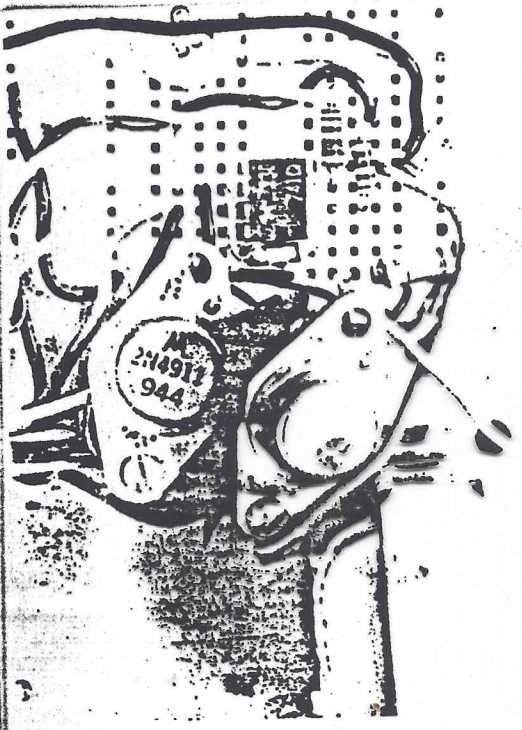
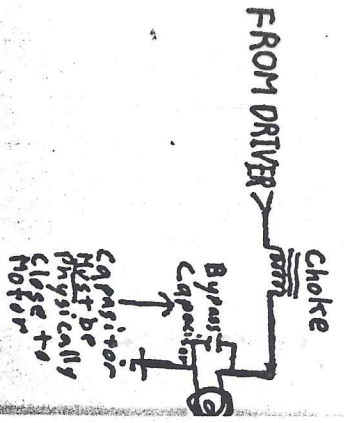
2



741 Truth TABLE

IN1	IN2	OUT
0	0	0
0	1	-15V
1	1	0
1	0	+15V

Projection Motor  
 and Motor Noise Elimination  
 Circuitry



DESIGN 3



of a pair of power transistors; an NPN and a PNP was the cheapest and most reliable solution (Figure 8 C).

A problem arised when the Reticcn array's circuit and the motor circuit were run simultaneously. The motor generated pulses on the power line which affected the timing circuits. A capacitor was put in parallel with the motor to bypass noise. Only when such a capacitor was placed directly on the motor was it effective. In other cases the lead wire in series with the capacitor acts as a resistor which gives the filter a time constant (RC). High frequency noise is unattenuated. A 0.2 microfarads (UF) bypass capacitor directly across the motor and an inductor in series with it together were effective in eliminating motor noise on the power supplies.

If a suitable computer is used, a program can run fast enough to leave the sensing system described above free running. The LDS could be calculated for the serial outputs of the elements of a light sensitive array with no backtracking. The National SCMP and the INTEL 8085 were 2 available computers. The speed of the 8085 was needed. 5204 Programmable Read Only Memory (PRCM) chips were used as program space. The 5204 PROM is not designed to run fast enough to be used with an 8085. It was found, however, that 5204s could be hand picked which would run fast enough to be acceptable. The computer which was used, an MCS 8085

development system, had 512 bytes of RAM, 6 ports and 512 bytes of program memory in the 5204 which was wired in as program space (Figure 7).

SOFTWARE

Our eyes contain "horizontal" and "amacrine" cells which exhibit lateral inhibition. These cells interact with rod and cone outputs to give an increased output on retinal ganglion cells when adjacent sensors have different light intensities illuminating them. The highest contrast image, the most focused in these cases, gives edge sensitive neurons the greatest output. When signals of this kind are most active in the fovea, the object focused on is in focus. In the periphery, areas with high activity of contrast sensitive "cells" indicate visual areas with a high amount of light level change or changes. A purpose in developing a serial focusing system was to simulate the lateral inhibition with successive difference measurements. Summing the absolute values of these differences gives the LDS. A program was written to maximize the sum of the absolute value of light level changes over the image plane (LDS) by focusing a lens in and out.

A package of programs was designed to develop, test and run the system. The routines of this program library were designed modularly to interdepend (see Appendix A for copies of the documented assembler language code). The copy used to run the programs resides as machine code in 5204 (a 512 byte PROM). The following is a list of the routines in this package, their purpose, design, and alternatives.

P R O G R A M SUTILITIES

This is a group of support programs. It is used extensively by the other programs in the system.

INIT

This routine is used to initialize the computer to be compatible with the hardware. It must be run before any other program in the package. To use any other routine in the library:

- 1) Set the 8085 stackpointer to 20C8.
- 2) Call INIT.
- 3) Call the routine to perform the desired function.

This routine initializes the motor direction constant to zero (stopped). It initializes the interrupt masks to off. It initializes ports:

21 is an input port. Its first bit is used to sense end of focus range.

22 is used as an output for transferring data to another device.

23 is an input port for the dataready input pulse.

29 is an output port. Its first 2 bits are used to run the motor.

2a is an input used to get the digitalized light level data.

2b is an input port whose low order bit is used to get the

start of array line reading pulse.

Design alternatives included the redundant practice of including this routine at the top of each high level routine (not enough space existed) or simply initializing the system in a user inputted routine.

#### GTSTRT

This routine is used by all routines which interface with the Reticon. It loops until the hardware gives a start of line pulse.

Alternate design would include interrupt driven software or replacing all of the timing circuitry in Figure 5 with software. It was unclear what computer was going to be made available for this project. To make the system most versatile; we made the interface machine independent.

#### GTRDY

This routine is used by all routines which use the Reticon array. It loops until an element is available for reading.

#### REGINIT

This routine zeros registers a, b, c, d and e.

#### MOTOR

This routine exclusive-ors the contents of the motor direction constant with 03. If the constant is 1 indicating forward focus, it changes it to 2 indicating reverse focus. If the constant is 2, it changes it to 1. When direction is changed the last Lateral Difference Sum (the focus constant) is set to zero. The motor control lines are found on bits 0 and 1 of port 29.

#### MINMAX

This routine is used to find the minimum and maximum light level elements in an array.

#### END

This routine is used to reverse the lenses direction at the end of its travel. When called, it pcls the first bit of port 21. If this bit is high, the routine reverses the direction of the motor.

DEMONSTRATION PROGRAMSDELAY

This routine waits for an amount of time controllable by registers D and E. It waits a time proportional to (FF-register E) (FF-register D) before returning. It also displays register E to the user. The routine is used to introduce hysteresis in focus programs. Register pair DE is the focus value, this routine will wait for a significant focus change to return, when focus is bad and will cause new focus state evaluation often when focus is close to being the best focus.

READEM

This routine reads light-level values from a user defined Reticon element with addresses between 0 and F. It writes out the elements' value and waits until the user either pushes the execute button or another address number to reread light level.

MOTDEM

This routine can be used to manually focus the lens or to test out the motor system. It simply reads a number from the users' input keyboard and outputs this value to the motor port continuously. It also writes the value to the Light Emitting Diode readout.

INPUT AND OUTPUTSTBUFF

This routine stores a table of light levels from the Ret-  
icon array in locations 2800 to 28FF. It waits for the  
start of line pulse, then begins to read data points. It  
reads the whole array.

HISTO

This routine puts out the numbers 00 to FF on port 21 the  
addresses of the data from locations 2800 to 28FF which it  
sends to port 22. The routine does this in an infinite loop  
so that if displayed as x and y on a scope the result is a  
histogram.



FOCUSERSSIMPLE FOCUS

This program focuses on a scene using MOTOR to change the direction of the focus motor when the program senses decreasing focus. It uses INIT to set up its constants and initialize hardware. Using preset constants for beginning of window and end of window the program gets a start of line pulse, counts ready pulses until the beginning of the window, and reads the rest of the line up to line length as data. The program uses the simple LDS algorithm to focus. It takes the absolute value of the difference in light level between successive elements and adds this to a 2 byte sum in registers D and E. This sum for each line read from the Reticon is compared to its predecessor unless the program has just changed focus direction.

At the end of each iteration, DELAY is called, a user defined program which delays change in focus direction inverse proportionally to the size of the focus metric LDS's magnitude.

FOCUS SQUARES

This program is used as an alternative to SIMPLE FOCUS. It is different in that it takes the square of the differences of light level to improve signal to noise ratio of the system: the LDSS. It uses a lookup table to take the squares. This lookup table is stored in user alterable memory (2800-28FF) (Figure 9). In this way other non-linear transformations can be tested easily.

AUTO FOCUS

This program varies from the other focusers in that it can average data over several elements and can change its focus window width to improve a scene's focusability. It will select a window including the minimum and maximum light intensities along the array. The program selects a resolution and window to focus through, using information from MINMAX about the minimum and maximum light levels seen in the scene. It makes this window overlap the minimum and maximum light level locations in a scene and 1/2 the distance between them on each end if possible.

Figure 9

"Fake Square"

Lookup Table  
Maps 0 → 7F  
onto 0 → 7F  
"Selecting" For  
larger numbers

	0	1	2	3	4	5	6	7
0	0	4	9	11	21	35	4A	61
1	0	4	9	12	22	36	4B	63
2	0	4	A	13	23	37	4D	65
3	0	5	A	14	24	39	4E	67
4	1	5	B	15	26	3A	50	69
5	1	5	B	16	27	3B	51	6B
6	1	6	C	17	28	3D	53	6D
7	1	6	C	18	29	3E	54	6F
8	2	7	D	19	2B	3F	56	71
9	2	7	D	1A	2C	41	57	73
A	2	7	E	1B	2D	42	59	75
B	2	7	E	1C	2E	43	5A	77
C	3	8	F	1D	30	45	5C	79
D	3	8	F	1E	31	46	5D	7B
E	3	8	10	1F	32	47	5F	7D
F	3	9	10	20	33	49	60	7E

Increment every  
4th 3rd 2nd 1st

Counting skips  
a number every  
4 3 2 1

7F 6F 5F 4F 3F 2F 1F 0F 7 6 5 4 3 2 1 0

RESULTS

After the system was complete, tests for its abilities were run to evaluate and improve it. LDS numbers were taken for stimuli of different spatial frequencies, including one single edge, 2 opposing edges, people, text and simple spatial frequencies up to 12 lines/cm. The focuser's step response (response for focusing stimuli presented initially out of focus) and tracking response (maximum speed for keeping moving stimuli in focus) were also evaluated.

The mount of the lens projecting the image onto the Reticon array was a problem. When the lens focus direction is changed; the track on which the lens moves allows the lens alignment to change. The lens has a gear rack on one side of it. When the motor pinion differentially loads the rack on the side of the lens, the play in the track is noticed as a rotation of the lens about a line perpendicular to its center line. The magnitude rotation is  $1/8$  degree ( $=0.125$  degrees/ $3.56$  degrees in field= $1/12$  of visual field). The alignment of the lens is held relatively constant if the motor direction is not changed. The motor reversing routine was altered to inhibit motor reversal immediately following a motor direction change. This insures that both LDS'S or LDSS'S being compared have been taken since the last motor change. This improved the stability of the focus considerably.

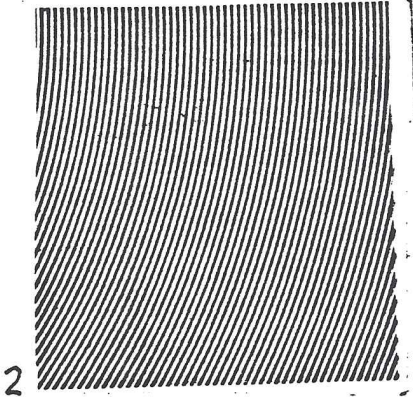
The speed of lens movement in focusing was measured to be about 1.5 mm/second. Its total range has been measured to be about 3 cm. This causes a limitation on the speed with which the system could focus and track a moving stimulus. The focus motor also has an onset latency. This is due to it being a direct current motor working against the inertia of the lens. It was found that focus change measurements had to be delayed just to get valid readings from 2 different focus positions. Using a delay proportional to (FF-low order byte) (FF-high order focus byte) sped focus. It allowed the system to focus large distances without interruption, when far away from best focus. As best focus was approached, the distance between focus reevaluation was decreased.

Three simple focus programs for the system were compared: OLD, NEW and SQUARE. OLD focuses making an Luminescence Differences Sum (LDS) which is composed of the sum of the difference of adjacent sensors. Its field of differences are non-overlapping. NEW, on the other hand computes the difference of all adjacent sensors by overlapping the differences. SQUARE allows the user to apply a lookup function located in the table starting at memory address 2800 to the differences in the LDSS. Because of time and memory constraints computation was confined to a 7 bit word. A function was placed in the SQUARE lookup-table which increases the increment between numbers mapped onto pseudo

quadratically (Figure 9). A 3.5 bit lookup table of squares was also tried. The lack of resolution more than outweighed the utility of the algorithm.

Analysis of the outputs of the imaging array on an oscilloscope was useful in obtaining information about imaging systems' limitations. Stimuli were first observed which had only high spatial frequency light level changes. Although when in focus they have large light level changes, when out of focus they may have no significant luminescence changes. From Figure 10; pictures 1, 2, 3, 5 and 8 are all examples of stimulus in this category. Picture 2 is the best example; when it is defocused 10 centimeters in the object plane, the image picked up by the imaging array appears to have imperceptible luminescence change (the change which makes focus possible). The other stimuli mentioned have the same problem. High spatial frequency stimuli have easily distinguishable luminescence change peaks when close to focus. It is not difficult to tell when they are in focus. It tends to be difficult to obtain best focus information for stimuli with low frequency luminescence changes. Their light level peaks are small and IDS comparisons are hard to make. Stimuli with mixed frequency light level changes have the sharp in-focus peaks and do not totally lose their contrast as quickly with defocus. From Figure 10 pictures 4, 6, 7 and 9 are all examples of stimuli in the mixed spatial frequency category. Picture 7, the best example of distrib-

Computer Cent  
**WORD PROC**  
 Use The Computer  
**SCRIPT Lectures**  
**FRESS Lectures**  
 Time 4:00 pm



3

terbions: tuq; bopticu; fion  
 gupdne; schafes; iniq;  
 biesenipou; incinqe; the pae  
 Ompel; issne; rdtessq; m  
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 reboliz; ou; znuq; to; the  
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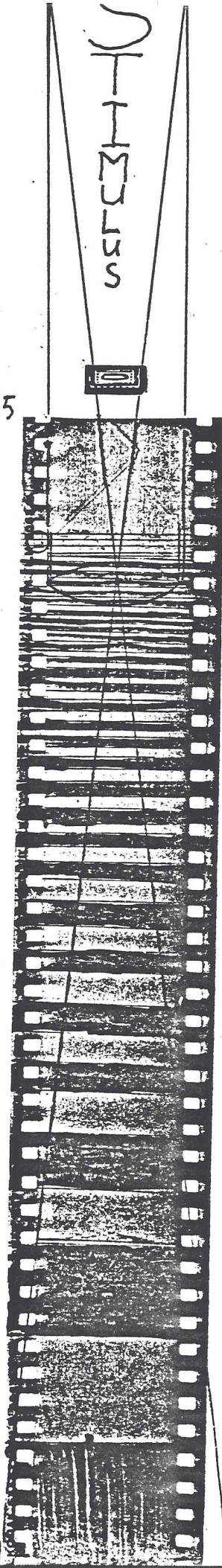
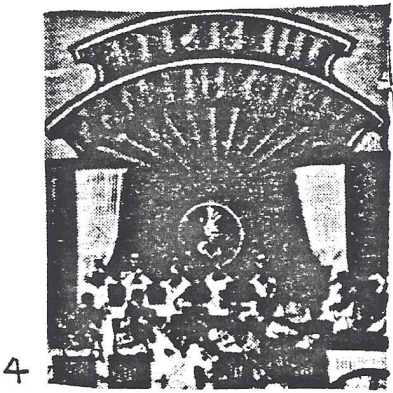
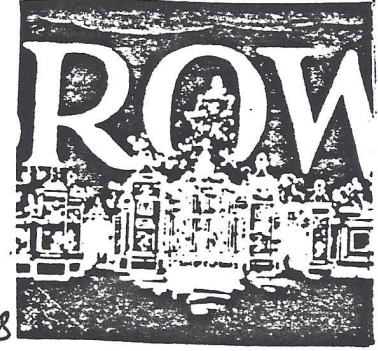
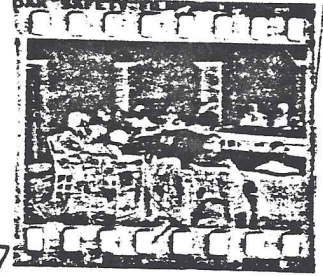


Figure 10



ution of spatial frequency, can be focused by the image based focusing system reliably from up to 30 centimeters defocused when presented at a 60 cm standard distance from the lens.



SYSTEM PERFORMANCE

All focus programs were shown to be able to find best focus on all of the stimulus material in Figure 10. Several system limitations were noted, and each of the programs performed better under different situations. High frequency stimulus was focused fastest using the NEW overlapping algorithm. The SQUARE algorithm only worked well with the function in Figure 9 as its "squared table" when the light level was high. This is because the function differentiates data best only for LDS focus numbers bigger than 3F. The non-overlapping algorithm (in OLD) works well for mixed stimuli. With this algorithm more space is left between numbers which are subtracted to make the LDS focus quality number.

Step response for stimulus (the amount of time required to focus a stimulus when initially presented in a defocused state) varied. When the DELAY program was used, fewer wrong decisions were made. If the stimulus was shown to the system within stable focus range (30 cm range at a standard 60 cm object distance for picture 6, 10 cm range at standard distance for picture 2) the focus time would be no more than double the time it took the motor to move to that position at full speed (6 seconds for picture 6). Wrong motor change decisions may be made by the focus algorithm before the system drives itself to within stable focus range. With

enough time, focus will be achieved (provided a good range of spatial frequencies is represented in the stimulus).

Tracking response is best for high frequency visual stimuli. This is because the change in LDS is greatest over focus change close to focus for visual stimulus with high spatial frequency. The focuser can track picture 2, for example, at faster than half the speed of the motor's lens position changing ability (1.5 mm/second). All stimuli in Figure 10 can be tracked close to  $1/2$  the speed of the motor's lens position changing ability.

DISCUSSION

The results of this autofocus project are extremely encouraging. The entire cost of this prototype Image Based Focusing system is well under \$500, including all optics and the sensor (which are needed for a camera anyway). The system can focus on a wide range of contrived and realistic stimuli. It can gauge light level, spatial frequency and find extremes of light intensity in its field. The system also has user-oriented software to manually focus, display individual image array elements in real time and to read in whole images. Additional software could utilize pattern recognition knowledge to find edges, which could rotate the camera for automatic tracking of moving objects.

The performance characteristics of the prototype described here are inadequate for commercial use. With the use of a faster focusing lens moving motor, the system would react proportionally faster (up to one focus change each thirtieth of one second (the time it takes to read the array)). With a better suited computer system and the algorithm could be more easily improved in resolution, could implement an LDSS square of differences algorithm and input two dimensional images.

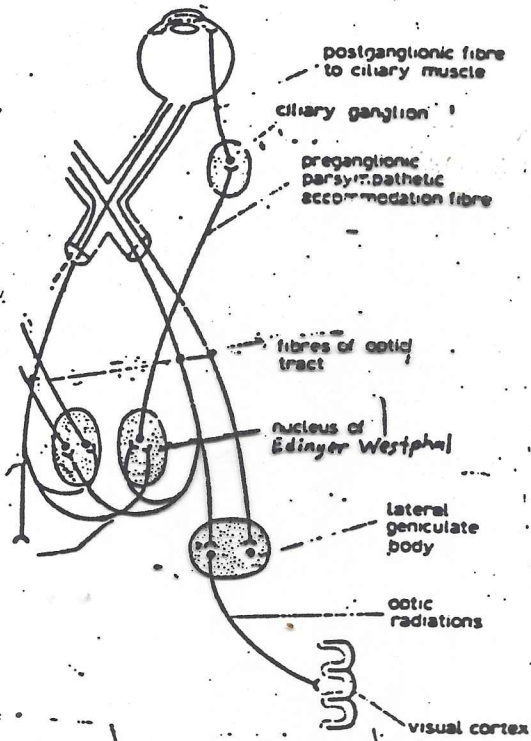
With these simple improvements, the focuser could focus at speeds competitive with the Visitronic and Polaroid system. Since the focusers' hardware is also a video camera, this system is a natural automatic focusing aid choice for video cameras.

The Luminescence Difference Sum bears close resemblance to known processing within animal's visual systems. Within the eye itself are photoreceptors and 3 layers of visual processing (Figure 11). The receptors (rods and cones) synapse (connect) with horizontal cells and bipolar cells. The horizontal cells synapse with more than one receptor and cause the receptive fields of bilateral cells to exhibit the first example of center-surround inhibition (the tendency for stimuli presented around the receptive field of a cell to inhibit its activity) in the visual system. This center-surround inhibition creates edge sensitivity in cell response. Amacrine cells synapse with more than one bipolar cells to introduce further laterally sensitive processing. The retinal ganglion cells connect to amacrine and bipolar cells to carry visual information along the visual tract. The sum of the outputs of 2 retinal ganglion cells with complementary center-surround responses corresponds to the absolute value of the difference in light level between these 2 fields. The sum of such responses in the foveal area (human area of high resolution vision) is the LDS. It could be maximized over change in accommodation which gives best

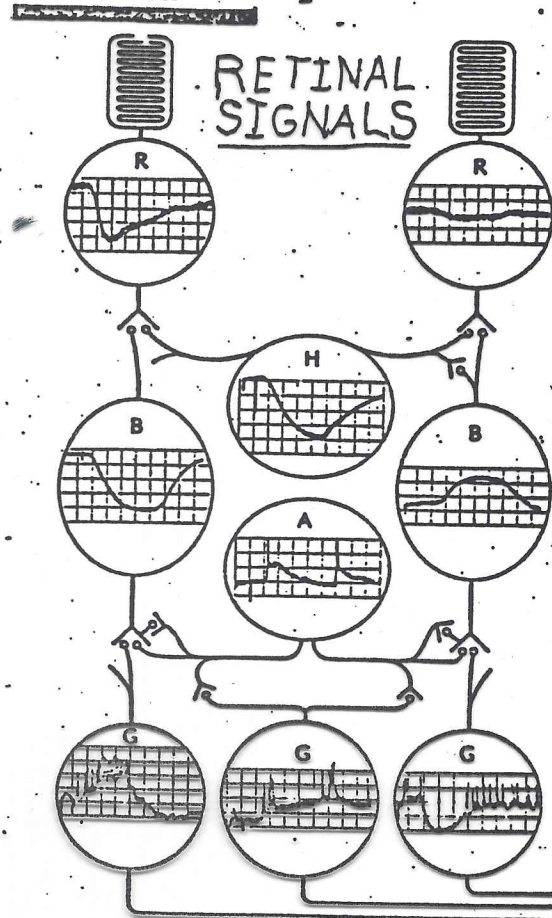
# Circuitry of The Retina and Focus

Figure 11.

## Visual Pathway

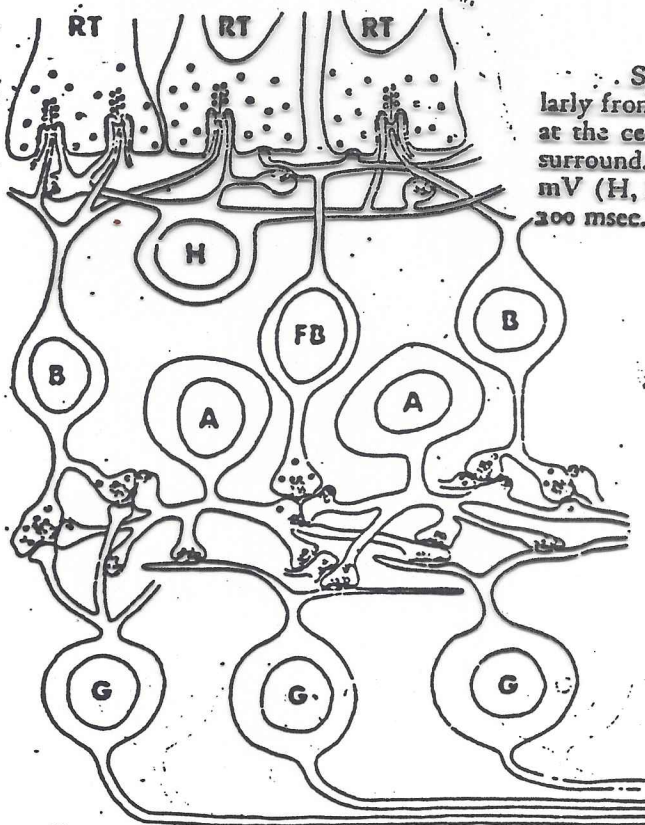


Pathways for the accommodation reflex modified after Wyburn, 1960, fig. 71, p. 98)



Synaptic actions in the vertebrate retina, as recorded intracellularly from neurons in *Necturus* (mudpuppy). Left, responses recorded at the center of a spot of light (bar above). Right, responses in the surround. Voltage calibrations, one scale division equals 1 mV (R); 2 mV (H, B, and G); 5 mV (A). Time calibration, one division equals 100 msec. (From Dowling, 1970, after Werblin and Dowling, 1969.)

## Retinal Connections



Vertebrate. A schematic drawing of the arrangements of synaptic contacts found in vertebrate retinas. In the outer plexiform layer, terminal processes of the bipolar cells (B) and horizontal cells (H) penetrate into invaginations in the receptor terminals (RT). The terminals of flat bipolar cells (FB) make superficial contacts on the bases of some receptor terminals. In the inner plexiform layer, two basic synaptic contacts appear to occur. Bipolar terminals may contact one ganglion cell (G) dendrite and one amacrine cell (A) process or bipolar

```

*****
:MINMAX
: THIS ROUTINE SCANS THE RETICCN'S ELEMENTS TO FIND THE BRIGHTEST
: & DULLEST PLACES. IT RETURNS MINIMUM BRIGHTNESS LEVEL IN REGISTER D
: MAXIMUM BRIGHTNESS LEVEL IN REGISTER E
: MINIMUM BRIGHTNESS ELEMENT'S ADDRESS IN LOCATION MIN (20C0),
: MAXIMUM BRIGHTNESS ELEMENT'S ADDRESS IN LOCATION MAX (MIN+1)
: INTERNALLY, REGISTER B IS USED FOR NEW DATA
: REGISTER C IS USED FOR NEW ADDRESSE
*****

```

```

*****
MINMAX 00 00 START
        21 LXI HL SET UP FOR MEMORY ACCESS OF MIN AND MAX
        C0
        20
        11 LXI DE INITIALIZE MIN=FF, MAX =0
        00
        7F
        0E MVI C ZERO ELEMENT COUNTER
        00 00
        CD CALL GET START OF SCAN PULSE
        GTSTRT
        00 00 REPEAT UNTIL END OF ARRAY
        CD CALL GET READY PULSE
        GTRDY
        DB IN GET ELEMENTS VALUE
        2A DATA
        47 MOV B A SAVE
        92 SUB D IF SMALLEST YET THEN (SUBTRACT MIN)
        E2 JP
        BIGR
        50 MOV D B MIN=NEW DATA
        71 MOV M C SAVE ADDRESS
        78 MOV A B
        C3 JMP
        ENDLP
        93 SUB E IF ACC BIGGER THEN
        FA JM
        ENDLP
        58 MOV E B MAX= NEW DATA
        23 INC HL SAVE ADDRESS
        71 MOV M C IN MAX
        2B DEC HL
        0C INC C INCREMENT ELEMENT COUNTER
        C2 JNZ END-LOOP
        NOTHER
        END C9 RET DONE

```

```

:*****
:READEM
:   THIS ROUTINE LETS A USER INPUT A NUMBER WHICH IS USED AS THE
: ADDRESS OF A LOCATION IN THE RETICON TO POLL.  THE LOCATION'S
: CONTENTS ARE DISPLAYED AND UPDATED CONTINUEOUSLY.
:

```

```

:*****
READEM  00    00                START
        CD    CALL              GET USER INPUT
        E7
        02
        47    MOV B A           PUT USERS ELEMENT INPUT
        4F    MOV C A           IN REGISTERS B AND C
R EAD   CD    CALL              GET START PULSE
        GTSTRT

ELEMNT  CD    CALL              REPEAT UNTIL USER SPECIFIED ELEMENT
        GTRDY                  GET READY PULSE

        05    DCR B            COUNT DOWN B TO USER SPECIFIED ELEMENT
        C2    JNZ              END-REPEATUNTIL ELEMENT
        ELEMNT

        DB    IN               READ DATA
        2A
        CD    CALL              DISPLAY DATA
        6E
        03
        41    MOV B C           UPDATE COUNTER
        C3    JMP              END
        READ

```

```

:*****
:MOTDEM
:   THIS PROGRAM LETS THE USER INPUT A NUMBER WHICH IS OUTPUTED TO
: THE MOTOR
:

```

```

:*****
MOTDEM  CD    CALL              START GET USER DATA
        E7                CALL READ KEYBOARD
        02
        CD    CALL              DISPLAY USER INPUT
        6E                CALL DISPLAY ROUTINE
        03
        D3                OUT DATA TO MOTOR
        29
        C3

MOTDEM

```

```

:*****
:HISTO
: THIS PROGRAM HISTOGRAMS DATA IN LOCATIONS 2800-28FF
: IT OUTPUTS X'S AT PORT 21 AND Y'S ATR 22
:
:*****

```

```

HISTO 21 LXI HL SET MEMOR READOUT AREA
      FF
      28
HIST 7E MOV A M GET PIECE OF DATA
      D3 OUT
      22
      7D MOV A L GET X
      D3 OUT
      21
      2D DEC L
      C2 JNZ END LOOP
      HIST
      C3 JMP END HISTO
      HISTO

```

```

:*****
:STBUFF
: THIS ROUTINE STORES A COPY OF THE BRIGHTNESSES OF ALL
: ELEMENTS OF THE RETICON AT LOCATIONS 2800-28FF.
:
:*****

```

```

STBUFF 00 00 START
        CD CALL INITIALIZE REGISTERS TO ZERO
        REGINIT
        21 LXI INITIALIZE MEMORY TO WRITE TO
        00
        28
        CD CALL GET START PULSE
        GTSTRT
ILL CD CALL GET READY PULSE
        GTRDY
        DB IN READ DATA
        2A
        77 MOV M A STORE RESULT
        23 INX H L INC MEMORY
        3E MOVI A IF END OF SCAN
        FF
        95 SUBT L
        C2 JNZ
        FILL
        C9 RET

```



```

:*****
:NEW SIMPLE FOCUS
:   THIS ROUTINE TAKES THE SUM OF SUCESSIVE DIFFERENCES OF THE
: SQUARES OF THE LIGHT LEVELS ON SUCCESSIVE
: ELEMENTS OF A 256 ELEMENT ARRAY.  THIS SUM IS COMPARED TO THE
: SUM TAKEN ON THE LAST ITERATION; TO MAXIMIZE CONTRAST WE ALLOW THE FO
: MOTOR TO CONTINUE IN THE SAME DIRECTION ONLY IF THE NEW SUM IS GREATE
: THE LAST.
: THE BEGINNING AND END POINTS OF THE SAMPLE ARE USER DEFINED (STORED I
: ATIONS )
: ROUTINES USED: 2090 ZERO REGISTERS
:                 2010 INITIALIZE SYSTEM
:                 2875 MOTOR DIRECTION CHANGE
: REGISTER USEAGE; A DATA AND COMPUTATION
:                   B +DATA AND START OF SCAN COUNTER
:                   C END OF SCAN COUNTER
:                   DE PRESENT SUCESSIVE DIFFERENCE SUM
:                   HL PAST SUCESSIVE DIFFERENCE SUM
:*****

```

```

START 00 NOOP BEGIN

      21 LXI H L INITIALIZE LAST DATA TO BAD FOCUS
      00 00
      00 00
      E5 PUSH
TOPTP CD CALL CALL INITIALIZE REGISTERS
      REGINIT

      0E LXI C LOAD END OF SCAN CONSTANT
      F0 FO *IMMEADIATE DATA*
      06 LXI B LOAD BEGINNING OF SCAN CONSTANT
      01 01 *IMMEADIATE DATA*
      CD CALL GET BEGINNING OF SCAN PULSE
      GTSTRT .

FNDBG 05 DEC B REPEAT UNTIL BEGINNING OF FOCUS AREA
      CA JZ <:EXIT IF DONE
      TOP

RDYBG CD CALL GET READY PULSE
      GTRDY

      C3 JMP END-REPEAT-BEGIN-OF-SCAN
      FNDBG

```

```

;*****
; DATA RETRIEVAL PORTION OF PROGRAM
;*****

```

```

      CD      CALL      GET FIRST ELEMENTS VALUE
      GTRDY           GET READY PULSE

      DB      IN        GET DATA
      2A
      47      MV B A    SAVE IT

TOP    CD      CALL      GET DATA
      GTRDY           GET READY PULSE
      DB      IN        GET DATA
      2A
      67      MV H A    SAVE DATA
      90      SUB B     TAKE DIFFERENCE
      44      MV B H
      F2      JP        IF NEGATIVE THEN
      POS

      EE      XRI           NEGATE TO MAKE POSITIVE (WE MAKE SUM
      FF      FF           OF INTENSITIY DIFFERENCES ULTIMATELY
POS    00      00          NOOP
      8B      ADC E      ADD TO SUCESSIVE DIFFERENCES
      5F      MOV E A    THIS, OUR MEGER CONTRIBUTION
      F2      JP        IF SUCESSIVE DIFFERENCE OVERFLOWS THEN
      NOV

      14      INC D      ADD 1 TO OVERFLOW SUCESSIVE OVERFLOW
      1E      MVI E      REZERO LOW CRDER BYTE
      00
NOV    0D      DCR C      IF NOT END CF FOCUS AREA THEN
      C2      JNZ       END-REPEAT-FOCUS
      TOP

```

:\*\*\*\*\*  
: COMPARE SUCCESSIVE DIFFERENCES FROM SUCCESSIVE FOCUS SAMPLES  
:\*\*\*\*\*

	E1	POP H L	GET LASTDATA
	D5	PUSH D E	SAVE NOW DATA
	7C	MV A H	
	92	SUB D	SUBTRACT SUCCESSIVE DIFFERENCES
	C2	JNZ	IF ANOTHER BYTE
	NOBTE		
	7D	MV A L	GET IT
	93	SUB E	COMPARE IT TOO
NOBTE	F4	CP	IF COMPARE IS PLUS THEN CALL MOTOR CHAN
	MOTOR		
	CD	CALL	CALL PRGRAM TO INTRODUCE HYSTERYSIS
	DELAY		
	C3	JMP	END-REPEAT-FOCUS
	TOPTP		

```

*****
: FOCUS TO USE SQUARED TABLE
: THIS ROUTINE TAKES THE SUM OF SUCESSIVE DIFFERENCES OF THE
: SQUARES OF THE LIGHT LEVELS ON SUCCESSIVE
: ELEMENTS OF A 256 ELEMENT ARRAY. THIS SUM IS COMPARED TO THE
: SUM TAKEN ON THE LAST ITERATION; TO MAXIMIZE CONTRAST WE ALLOW THE FO
: MOTOR TO CONTINUE IN THE SAME DIRECTION ONLY IF THE NEW SUM IS GREATER
: THE LAST.
: THE BEGINNING AND END POINTS OF THE SAMPLE ARE USER DEFINED (STORED IN
: ATIONS )
: ROUTINES USED: 2090 ZERO REGISTERS
:                2010 INITIALIZE SYSTEM
:                2875 MOTOR DIRECTION CHANGE
: REGISTER USEAGE: A DATA AND COMPUTATION
:                  B +DATA AND START OF SCAN COUNTER
:                  C END OF SCAN COUNTER
:                  DE PRESENT SUCESSIVE DIFFERENCE SUM
:                  HL PAST SUCESSIVE DIFFERENCE SUM
*****

```

```

*****
START 00 NOOP BEGIN
      21 LXI H L INITIALIZE LAST DATA TO BAD FOCUS
      00 00
      00 00
      E5 PUSH
TOPTP CD CALL CALL INITIALIZE REGISTERS
      REGINIT
      0E LXI C LOAD END OF SCAN CONSTANT
      FO FO *IMMEADIATE DATA*
      06 LXI B LOAD BEGINNING OF SCAN CCNSTANT
      01 01 *IMMEADIATE DATA*
      CD CALL GET BEGINNING OF SCAN PULSE
      GTSTRT .
FNDBG 05 DEC B REPEAT UNTIL BEGINNING OF FOCUS AREA
      CA JZ <:EXIT IF DONE
      TOP
RDYBG CD CALL GET READY PULSE
      GTRDY
      C3 JMP END-REPEAT-BEGIN-OF-SCAN
      FNDBG

```

```

:*****
: DATA RETRIEVAL PORTION CF PROGRAM
:*****

```

```

CD    CALL          GET FIRST ELEMENTS VALUE
GTRDY          GET READY PULSE

DB    IN           GET DATA
2A
47    MV B A

```

```

TOP    CD    CALL          GET DATA
      GTRDY          GET READY PULSE
      DB    IN           GET DATA
      2A
      67    MV H A
      90    SUB B
      44    MV B H
      F2    JP           IF NEGATIVE THEN
      POS

```

```

      EE    XRI          NEGATE TO MAKE POSITIVE (WE MAKE SUM
      FF    FF          OF INTENSITIY DIFFERENCES ULTIMATELY
POS    00    00          NOOP
      CD    CALL          SQUARE DIFFERENCE
      SQR
      8B    ADC E
      5F    MOV E A
      F2    JP           ADD TO SUCESSIVE DIFFERENCES
      NOV          THIS, OUR MEGER CONTRIBUTION
                        IF SUCESSIVE DIFFERENCE OVERFLOWS THEN

```

```

NOV    14    INC D
      0D    DCR C
      C2    JNZ
      TOP          ADD 1 TO OVERFLOW SUCCESSIVE OVERFLOW
                        IF NOT END OF FOCUS AREA THEN
                        END-REPEAT-FOCUS

```

\*\*\*\*\*  
: COMPARE SUCCESSIVE DIFFERENCES FROM SUCCESSIVE FOCUS SAMPLES  
\*\*\*\*\*

	E1	POP H L	GET LASTDATA
	D5	PUSH D E	SAVE NOW DATA
	7C	MV A H	
	92	SUB D	SUBTRACT SUCCESSIVE DIFFERENCES
	C2	JNZ	IF ANOTHER BYTE
	NOBTE		
	7D	MV A L	GET IT
	93	SUB E	COMPARE IT TOO
NOBTE	FC	CM	IF COMPARE IS MINUS THEN CALL MOTOR CHAN
	MOTOR		
	C3	JMP	END-REPEAT-FOCUS
	TOPTP		

```

*****
* DELAY
* THIS ROUTINE IS USED BY FOCUS PROGRAMS TO DELAY BETWEEN FOCUS
* DECISIONS INVERSELY PROPORTIONALLY TO THE FOCUS CONSTANT THE
* FOCUS PROGRAM HAS AS ITS MEASURE OF FOCUS. IN THIS WAY THE
* PROGRAM FOCUSES FARTHER BETWEEN REEVALUATIONS OF FOCUS DIRECTION
* WHEN IT IS FAR AWAY FROM FOCUS THAN WHEN IT IS CLOSE TO BEST FOCUS.*
*
*****

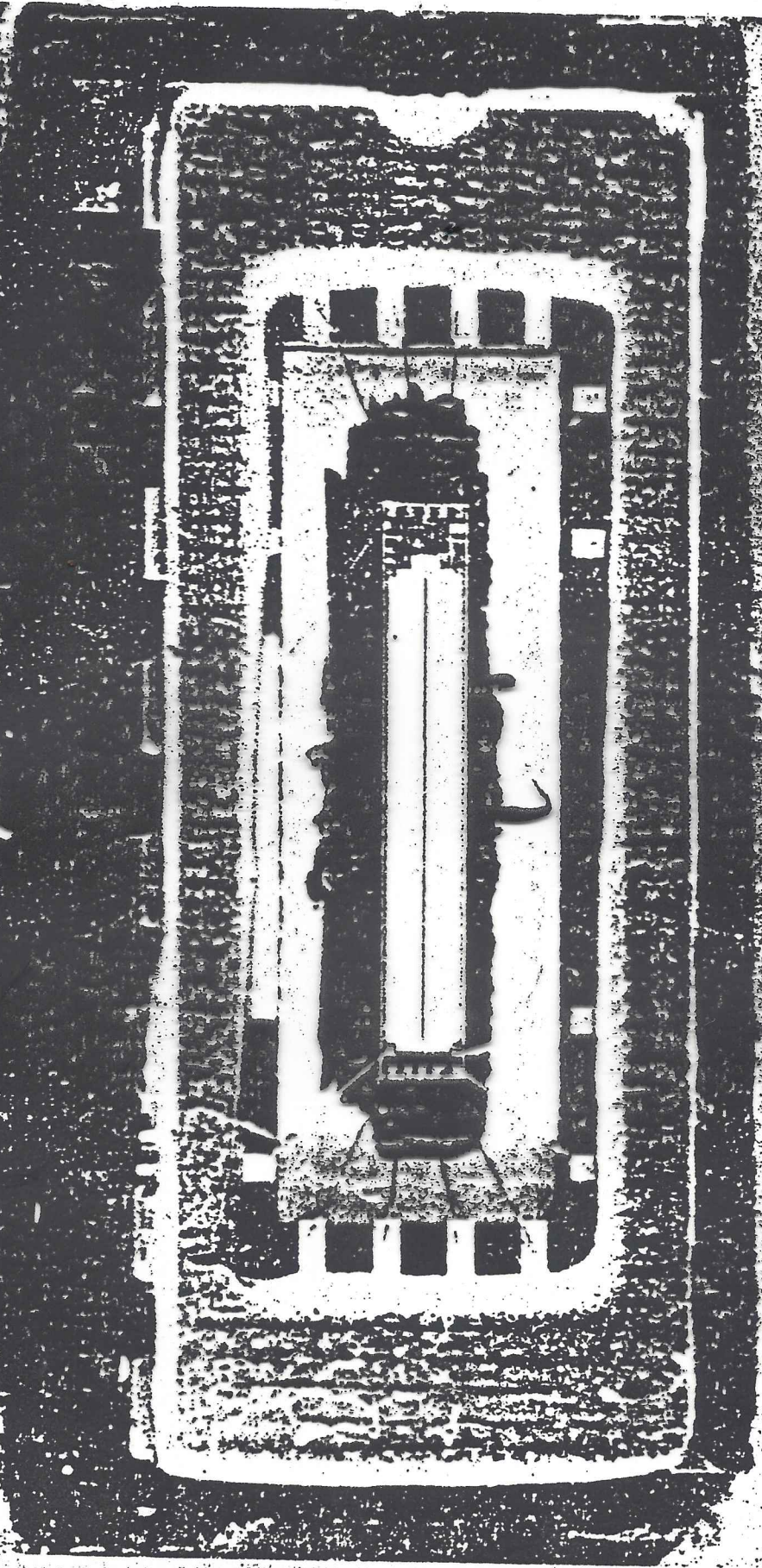
```

```

DELAY      00      NOOP              BEGIN
           00      NOOP
           00      NOOP
           D5      PUSH DE          SAVE FOCUS LDQ
           7B      MV A E          DISPLAY LDQ
           CD      CALL
           6E
           03
           D1      POP DE          RESTORE FOCUS LDQ
           00      NOOP
           4A      MV C D          GET LOOP CCNSTANT= HIGH ORDER OF LDQ{
OLOOP      7B      MV AE          REPEAT UNTIL HIGH ORDER LDQ
ILOOP      3C      INC A          REPEAT UNTIL LOW ORDER LDQ
           C2      JNZ            ENDLOOPI
ILOOP
           0C      INC C
           C2      JNZ            ENDLOOP
OLOOP
           C9      RET            END

```

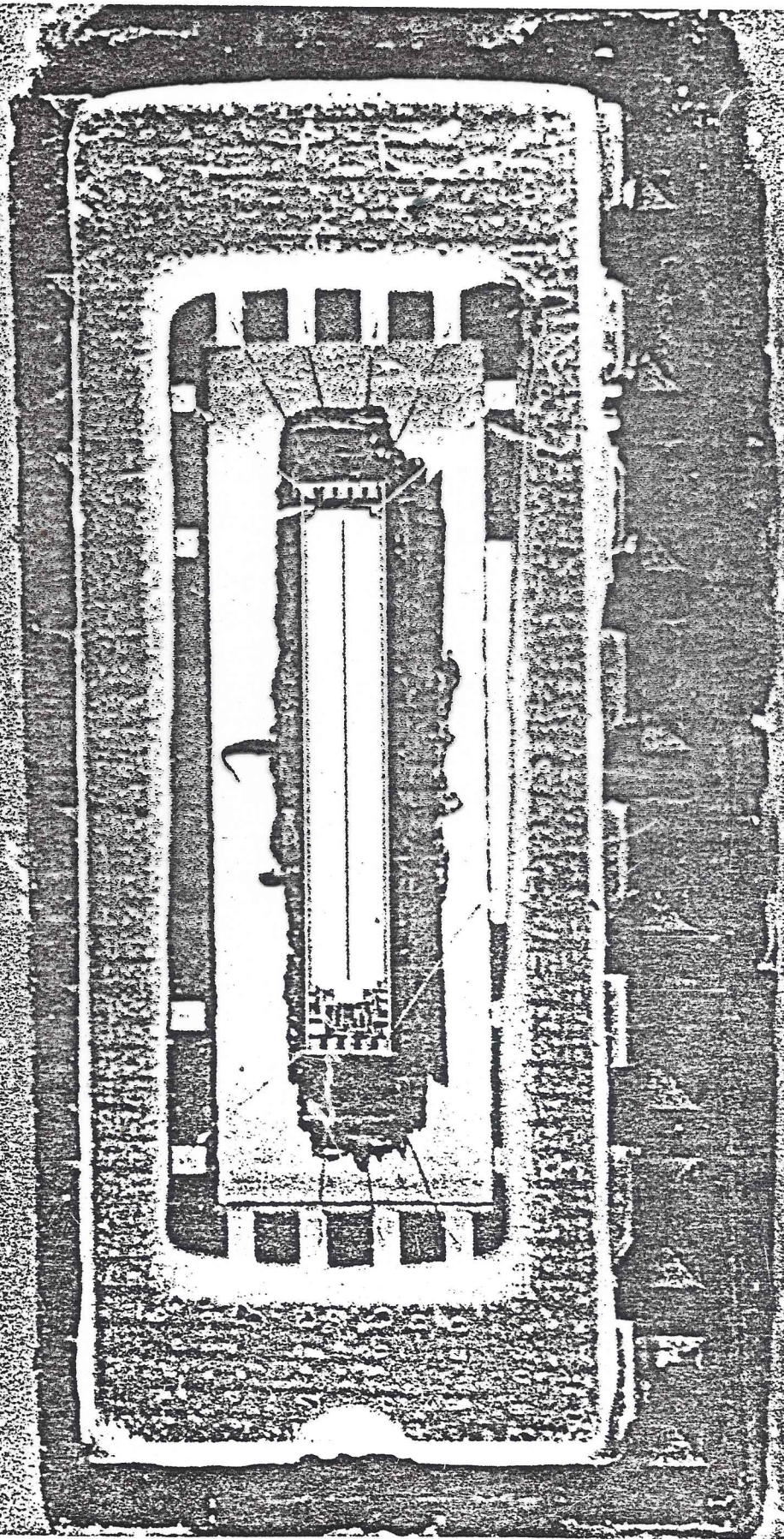
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16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1



1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16